



TEA: Test-time Energy Adaptation

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Paper



Code



Presenter: Yige Yuan (袁一歌)

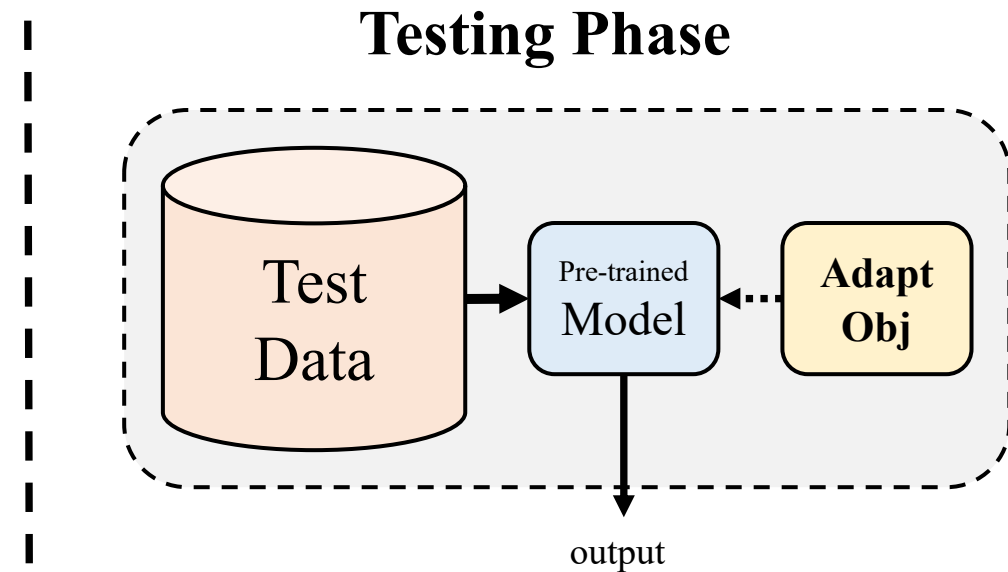
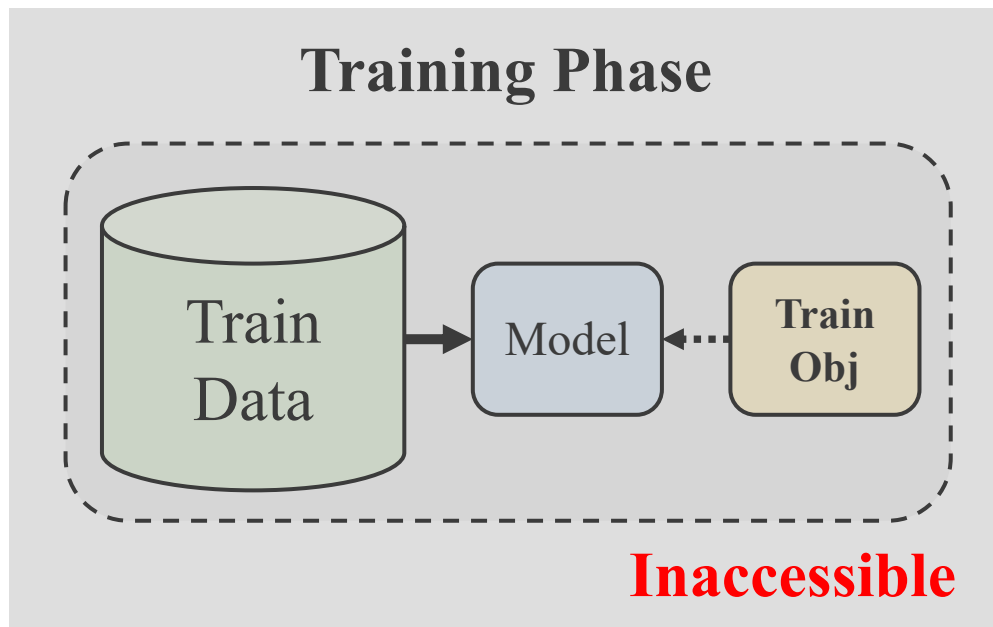
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- **Motivation**
- Method
- Experiments

MOTIVATION

Test-time Adaptation

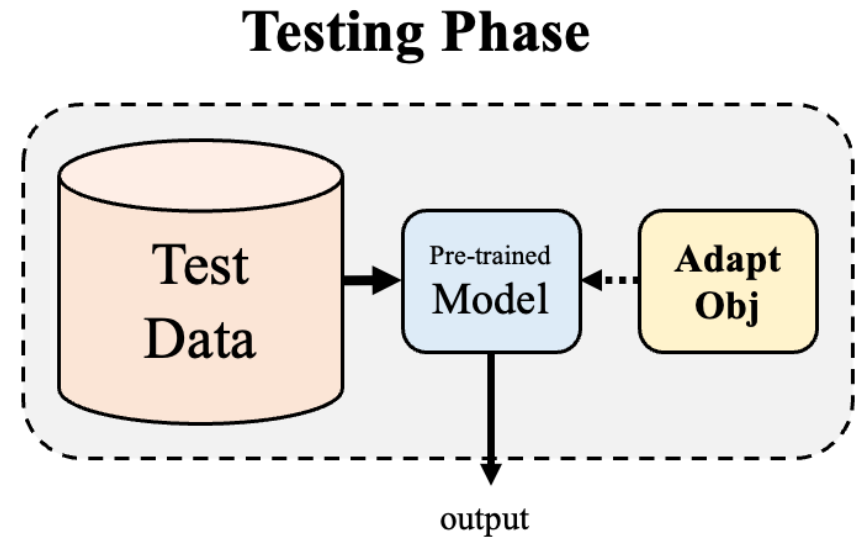
- Inaccessible training data and training procedure.
- Adapting a pre-trained model with test data.



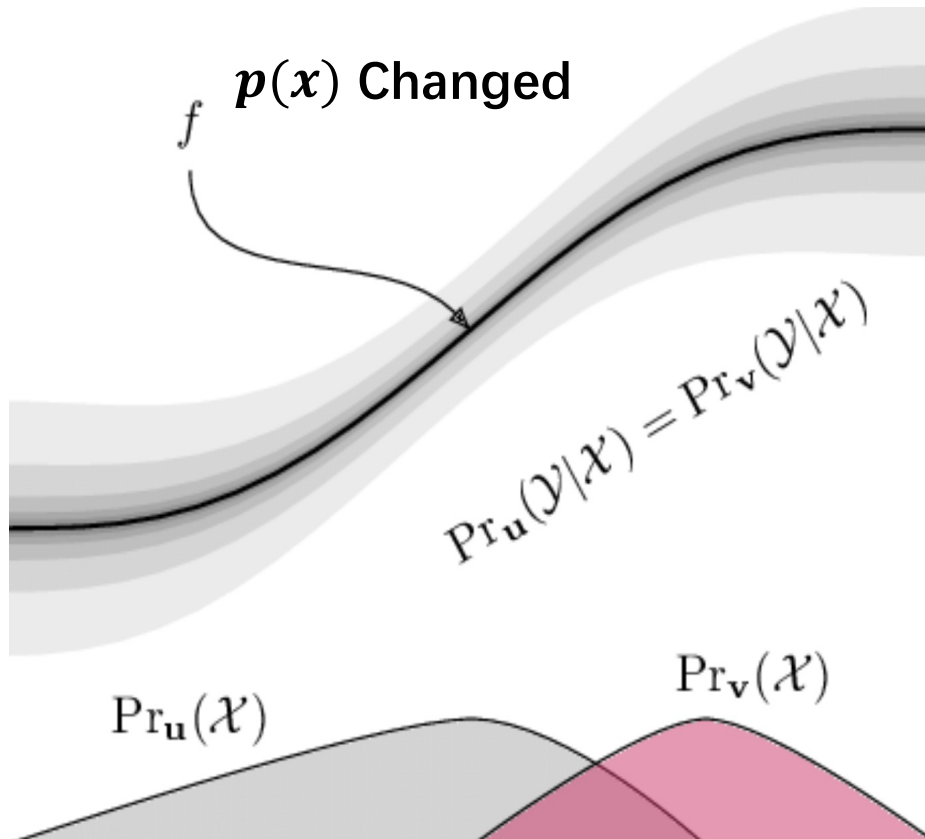
MOTIVATION

Related Work

- Entropy-based TTA
 - Minimize the prediction entropy.
 - TENT, ETA, EATA, SAR
- Pseudo-labeling-based TTA
 - Utilize test-time generated labels for updates.
 - PL, SHOT
- Consistency-based TTA
 - Constraint consistency across augmented samples.
 - MEMO, AdaContrast
-



MOTIVATION



Covariate Shift

- the decrease in generalization ability on test data with distribution shift can be attributed to the model's reliance on the marginal distribution of the training data
- They do not address the marginal distribution shift $p(x)$, impairing model calibration and introducing confirmation bias.

How to perceive marginal distribution $p(x)$?

MOTIVATION

Energy Based Model

- **What is? A Non-normalized Probabilistic Model**

the energy function maps each sample into an energy that can be considered as an unnormalized probability, with lower scores indicating higher likelihoods

$$E_{\theta}(\mathbf{x}) : R^D \rightarrow R$$

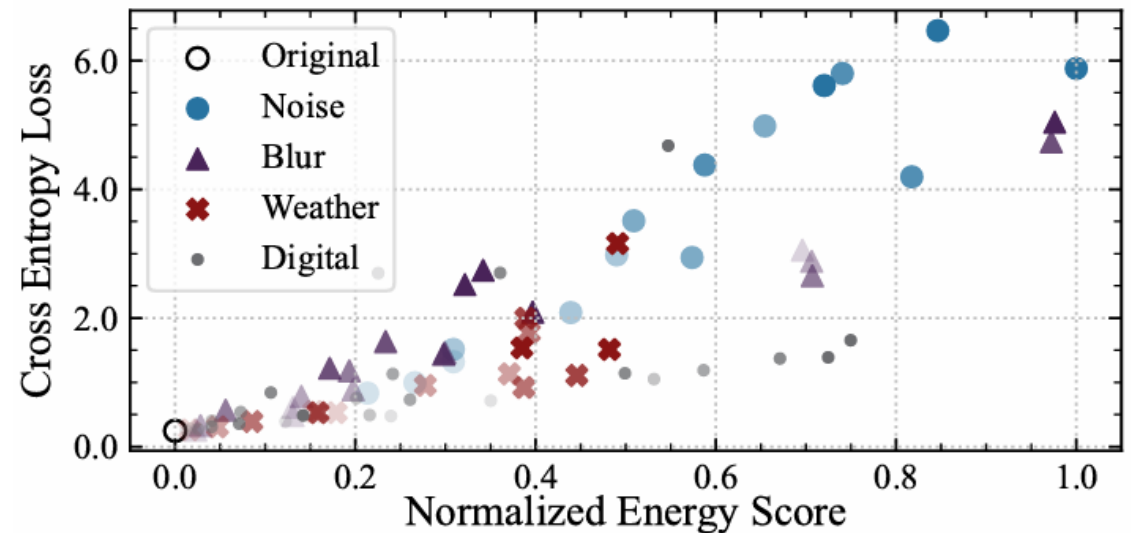
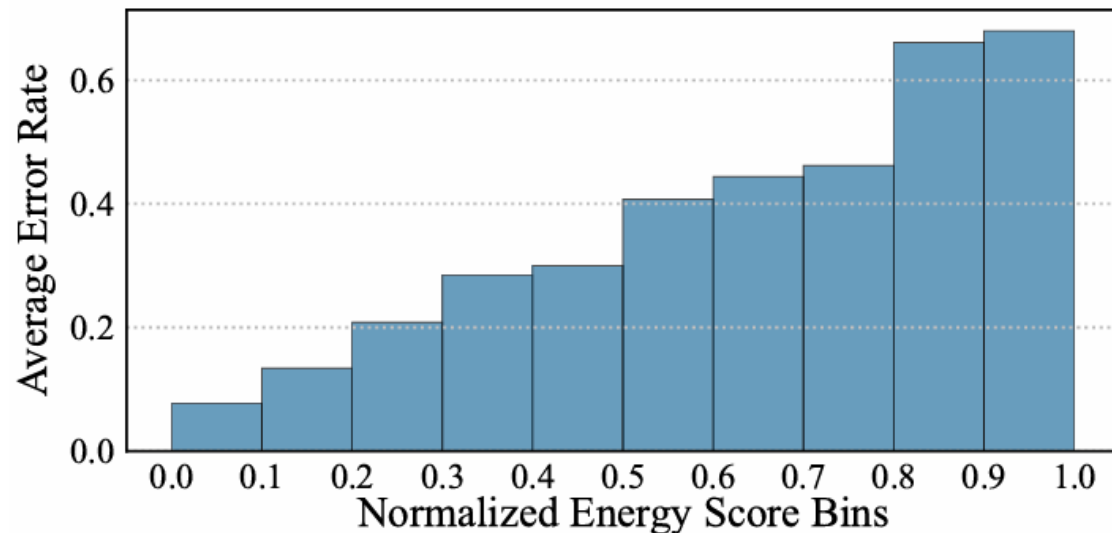
$$p_{\theta}(\mathbf{x}) = \frac{\exp(-E_{\theta}(\mathbf{x}))}{Z_{\theta}}$$

$$Z_{\theta} = \int \sum_y \exp(f_{\theta}(\mathbf{x})[y]) d\mathbf{x}$$

MOTIVATION

How **Energy** related to **Generalization**

- Our Observation
 - Low energy = high probability, high performance
 - High energy = low probability, low performance



- Motivation
- **Method**
- Experiments

METHOD

Overall idea

Enhancing the model's perception of test distribution from an energy-based perspective, involving two key steps:

- treating the Pretrained Classifier as the energy-based model
- optimizing it to perceive test data by decreasing the energy

Notation

Labeled training data $(x, y) \sim P_{\text{train}}(x, y)$

Unlabeled test data $x \sim P_{\text{test}}(x)$

Pre-trained Classifier $f_{\theta}: X \rightarrow Y$

Inaccessible

Accessible

Accessible

METHOD

Treating Classifier **as** EBM

Pretrained Classifier

↓
introduce unknown
normalizing constant Z_θ

↓
marginalize out y

↓
substitute E_θ

Energy Based Model

$$p_\theta(y | \mathbf{x}) = \frac{\exp(f_\theta(\mathbf{x})[y])}{\sum_{y'} \exp(f_\theta(\mathbf{x})[y'])}$$

$$p_\theta(\mathbf{x}, y) = \frac{\exp(f_\theta(\mathbf{x})[y])}{Z_\theta}$$

$$p_\theta(\mathbf{x}) = \sum_y p_\theta(\mathbf{x}, y) = \frac{\sum_y \exp(f_\theta(\mathbf{x})[y])}{Z_\theta}$$

$$p_\theta(\mathbf{x}) = \frac{\exp(-E_\theta(\mathbf{x}))}{Z_\theta}$$

$$E_\theta(\mathbf{x}) = -\log \sum_y \exp(f_\theta(\mathbf{x})[y])$$

A Pre-Trained Classifier can be reinterpreted as an Energy Based Model

METHOD

Inject Test Distribution into Classifier

Our Objective:

Test Data

$$\max p_{\theta}(\mathbf{x}_{\text{test}})$$

Classifier's Inherent Distribution

Modeling Test Distribution under Pre-trained Classifier

$$p_{\theta}(\mathbf{x}_{\text{test}}) = \frac{\exp(-E_{\theta}(\mathbf{x}_{\text{test}}))}{Z_{\theta}}$$

$$Z_{\theta} = \int \sum_y \exp(f_{\theta}(\mathbf{x})[y]) d\mathbf{x}$$

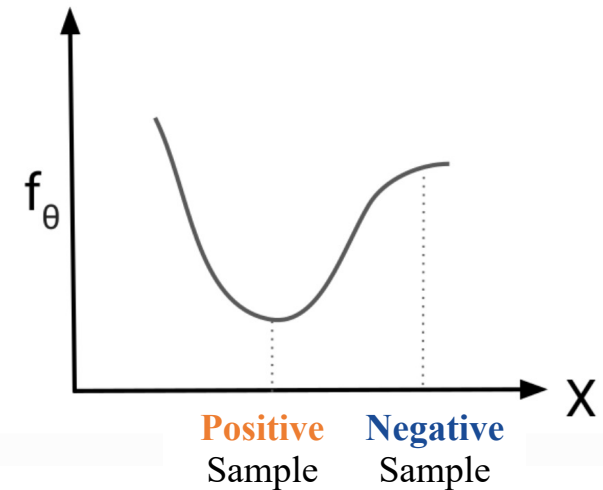
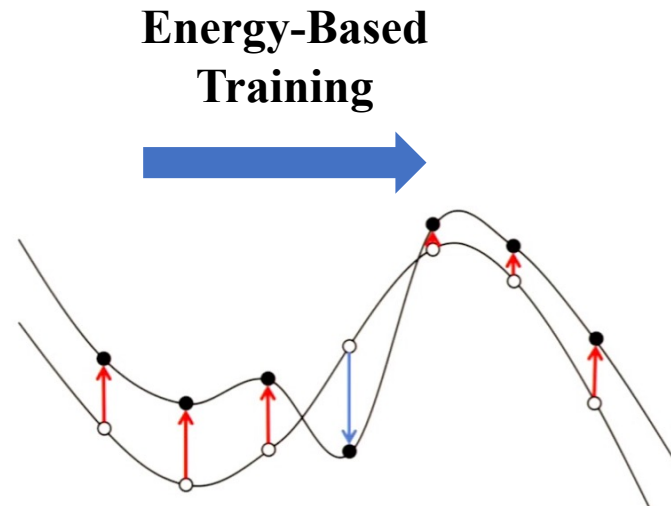
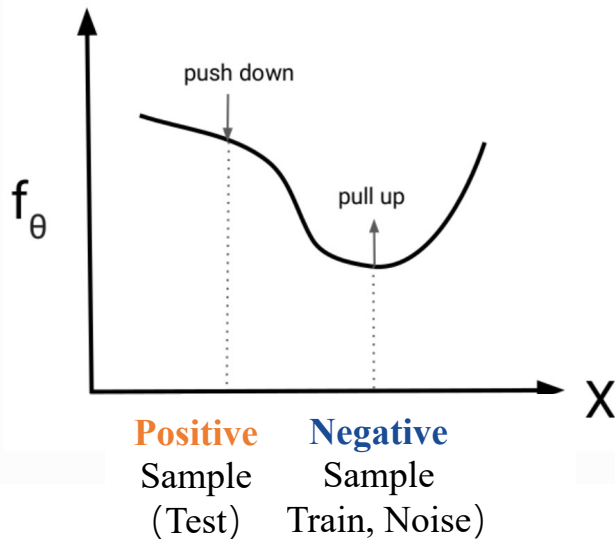
Computing Z requires integrating all x, How to Optimize?

METHOD

Inject Test Distribution into Classifier

Contrastive Divergence

$$\frac{\partial \log p_{\theta}(\mathbf{x}_{\text{test}})}{\partial \theta} = \mathbb{E}_{\tilde{\mathbf{x}} \sim p_{\theta}} \left[\frac{\partial E_{\theta}(\tilde{\mathbf{x}})}{\partial \theta} \right] - \frac{\partial E_{\theta}(\mathbf{x}_{\text{test}})}{\partial \theta}$$



Inject Test Distribution into Classifier

Test Distribution Injection: $\max_{p_\theta}(\mathbf{x}_{\text{test}})$
Classifier's Inherent Distribution

Contrastive Divergence

$$\frac{\partial \log p_\theta(\mathbf{x}_{\text{test}})}{\partial \theta} = \mathbb{E}_{\tilde{\mathbf{x}} \sim p_\theta} \left[\frac{\partial E_\theta(\tilde{\mathbf{x}})}{\partial \theta} \right] - \frac{\partial E_\theta(\mathbf{x}_{\text{test}})}{\partial \theta}$$

Stochastic Gradient Langevin Dynamics

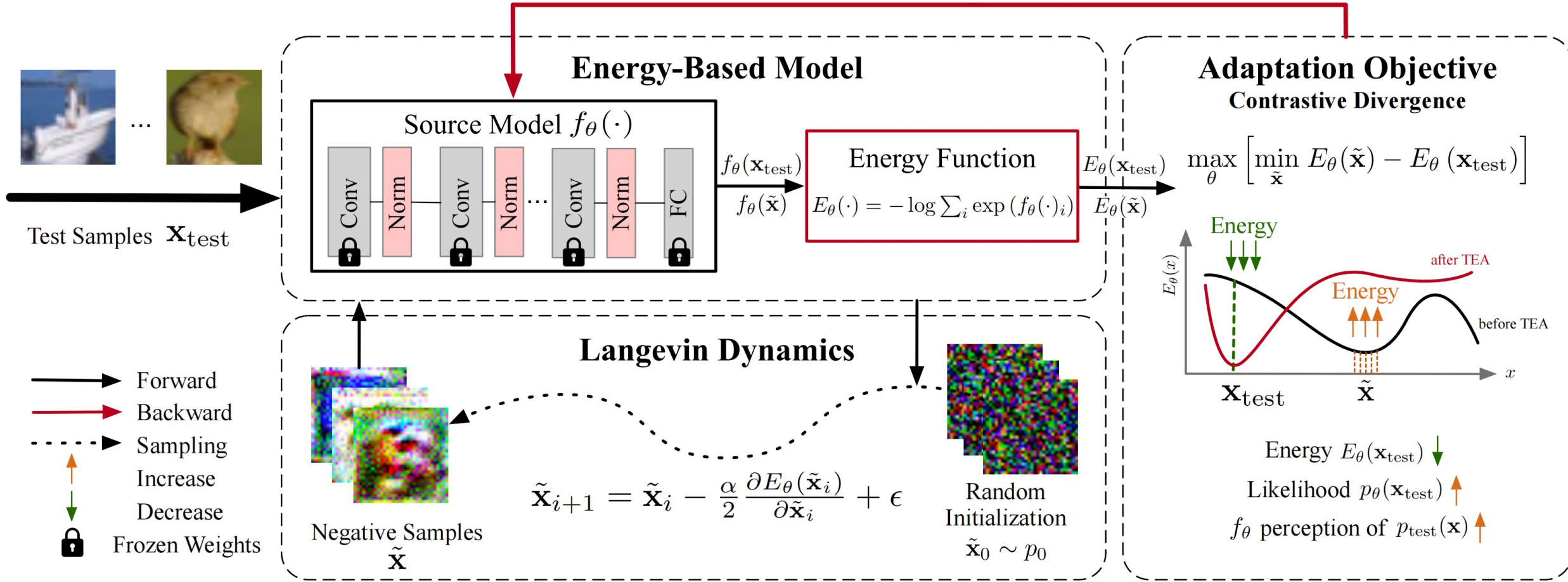
$$\tilde{\mathbf{x}}_{t+1} = \mathbf{x}_t - \frac{\alpha}{2} \frac{\partial E_\theta(\tilde{\mathbf{x}}_t)}{\partial \tilde{\mathbf{x}}_t} + \sqrt{\alpha} \epsilon, \quad \epsilon \sim \mathcal{N}(\mathbf{0}, \mathbf{I}),$$

Overall Objective

$$\max p_\theta(\mathbf{x}_{\text{test}}) = \max_\theta [\min_{\tilde{\mathbf{x}}} E_\theta(\tilde{\mathbf{x}}) - E_\theta(\mathbf{x}_{\text{test}})]$$

METHOD

Test-Time Energy Adaptation



- Motivation
- Method
- **Experiments**

EXPERIMENTS

Experimental Settings

- **Datasets**

- 15 shift corruption distributions by **CIFAR-10(C)**, **CIFAR-100(C)**, and **Tiny-ImageNet(C)**.
- 4 domains in the PCAS dataset: **Photo**, **Art**, **Cartoon**, and **Sketch**.

- **Baselines**

- Without TTA: **Source**
- Norm Based TTA: **BN DUA**
- Pseudo Label Based TTA: **PL**, **SHOT**
- Entropy Based TTA: **TENT**, **ETA**, **EATA**, **SAR**

- **Metrics**

- **Accuracy** on clean data.
- **Average Accuracy** and **mCE** across all severity levels and at the severest level.

EXPERIMENTS

Image Corruption Scenario Performance

Table 1. Comparisons of TEA and baselines for image corruption on CIFAR-10(C), CIFAR-100(C), and Tiny-ImageNet(C) using WRN-28-10 with BatchNorm. Accuracy and mCE are evaluated at the most severe level and across all levels with asterisk (*) indicating the results are taken from the original paper [56]. The best adaptation results are highlighted in **boldface**.

WRN-28-10 BatchNorm		CIFAR-10(C)					CIFAR-100(C)					Tiny-ImageNet(C)				
		Clean	Corr Severity 5		Corr Severity 1-5		Clean	Corr Severity 5		Corr Severity 1-5		Clean	Corr Severity 5		Corr Severity 1-5	
		Acc (↑)	Acc (↑)	mCE (↓)	Acc (↑)	mCE (↓)	Acc (↑)	Acc (↑)	mCE (↓)	Acc (↑)	mCE (↓)	Acc (↑)	Acc (↑)	mCE (↓)	Acc (↑)	mCE (↓)
Source		94.77	56.47	100.00	73.45	100.00	81.79	35.39	100.00	52.12	100.00	63.19	21.21	100.00	34.13	100.00
Norm	BN [52]	93.97	79.56	52.65	85.63	60.00	80.83	60.06	63.54	68.11	69.42	45.04	27.74	93.42	34.27	100.96
	DUA* [41]	-	80.10	50.78	-	-	-	-	-	-	-	-	-	-	-	-
Pseudo	PL [34]	93.75	51.42	106.98	72.62	99.37	80.52	53.40	72.12	64.53	75.29	47.84	28.26	91.22	39.83	91.67
	SHOT [36]	93.25	74.77	63.19	82.35	72.61	80.52	56.53	68.01	66.00	73.28	47.95	29.14	90.16	40.01	91.41
Entropy	TENT [60]	93.66	81.41	48.13	86.75	56.17	80.14	63.09	59.42	69.47	67.80	39.54	26.31	95.52	32.03	104.49
	ETA [45]	93.96	79.58	52.64	85.63	59.99	80.65	59.82	64.52	67.17	72.40	43.20	27.28	94.12	33.46	102.25
	EATA [45]	93.96	79.59	52.62	85.64	59.98	80.68	60.24	63.75	67.48	71.66	43.42	27.28	94.09	33.47	102.24
	SAR [46]	93.97	79.77	51.94	85.83	58.97	80.84	62.95	59.37	70.01	65.99	41.58	28.21	92.82	34.60	100.47
Energy	TEA	94.09	83.34	43.69	87.88	52.00	80.88	65.10	56.18	71.22	63.74	51.65	31.67	87.99	39.96	92.12

Figure: Adaptation performance under image corruption scenarios using BatchNorm

EXPERIMENTS

Image Corruption Scenario Performance

Table 2. Comparisons for image corruption on CIFAR-10(C), CIFAR-100(C), and Tiny-ImageNet(C) using ResNet-50 with GroupNorm across all severity levels. Best results are in **boldface**.

ResNet50 GroupNorm		CIFAR-10(C)		CIFAR-100(C)		Tiny-ImageNet(C)	
		Acc (↑)	mCE (↓)	Acc (↑)	mCE (↓)	Acc (↑)	mCE (↓)
Source		78.71	100.00	54.98	100.00	26.64	100.00
Pseudo	PL	79.43	94.76	56.68	96.02	26.60	99.92
	SHOT	81.98	86.65	58.31	93.45	29.11	96.73
Entropy	TENT	77.29	102.88	56.34	96.88	26.65	99.94
	ETA	78.68	100.09	56.72	96.37	29.25	96.42
	EATA	78.70	100.02	56.76	96.28	29.25	96.42
	SAR	78.78	99.65	55.28	99.33	27.05	99.41
Energy	TEA	83.05	79.09	59.67	89.32	30.41	94.81

Figure: Adaptation performance under image corruption scenarios using GroupNorm

EXPERIMENTS

Domain Generalization Scenario Performance

Table 3. Single source domain generalization comparisons on PACS datasets using ResNet-18 with BatchNorm in terms of Accuracy. The best adaptation results are highlighted in **boldface**.

Source Domain	Method	Target Domain				Avg
		Photo	Art	Cartoon	Sketch	
Photo	Source	-	26.76	22.40	16.62	21.93
	BN	-	26.66	27.94	15.96	23.52
	TENT	-	26.95	29.86	17.54	24.78
	EATA	-	26.66	28.11	15.98	23.59
	SAR	-	26.71	28.41	15.98	23.70
	SHOT	-	26.61	29.86	20.92	25.80
	TEA	-	28.81	33.62	20.49	27.64
	Art	Source	49.04	-	36.43	24.48
BN		46.65	-	28.28	22.73	32.55
TENT		50.78	-	30.12	24.61	35.17
EATA		46.83	-	29.31	23.42	33.19
SAR		47.90	-	33.02	26.27	35.73
SHOT		50.24	-	34.30	29.37	37.97
TEA		56.29	-	38.57	28.71	41.19
Cartoon		Source	42.69	29.79	-	29.47
	BN	28.68	25.15	-	20.87	24.90
	TENT	30.96	23.34	-	22.65	25.65
	EATA	28.80	25.10	-	25.04	26.31
	SAR	29.70	25.78	-	21.51	25.66
	SHOT	37.72	22.66	-	23.14	27.84
	TEA	36.05	31.44	-	22.88	30.12
	Sketch	Source	19.94	18.70	32.21	-
BN		13.47	17.14	29.86	-	20.16
TENT		13.53	17.38	29.52	-	20.14
EATA		13.17	17.33	30.08	-	20.19
SAR		13.29	18.80	29.95	-	20.68
SHOT		19.76	18.75	30.46	-	22.99
TEA		19.64	21.24	33.19	-	24.69

Figure: Adaptation performance under domain generalization scenarios

EXPERIMENTS

Energy Reduction & Generalizability Enhancement

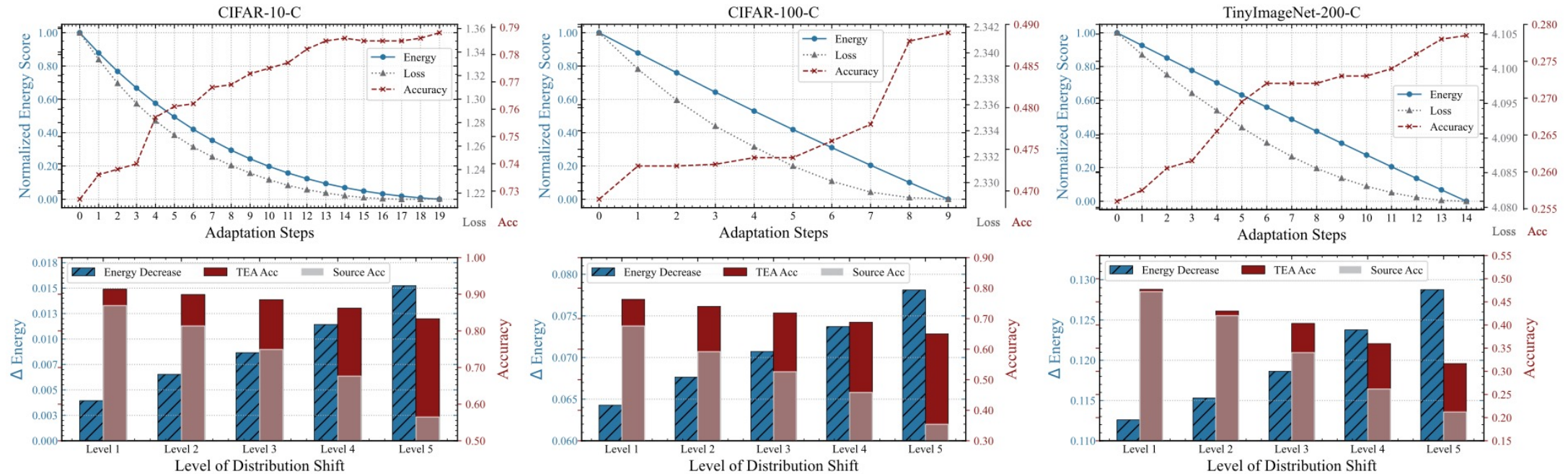


Figure 3. This illustration captures the energy reduction and generalizability enhancement achieved by TEA across CIFAR-10-C, CIFAR-100-C, and TinyImageNet-200-C, displayed from left to right. The **upper** set of graphs trace the evolution of energy score, corresponding loss and accuracy in response to incrementally increasing TEA adaptation steps. The **lower** set uncovers the extent of energy reduction and the consequent performance improvement before and after executing TEA adaptation, under different levels of distribution shift.

Figure: Relation between energy reduction and generalizability enhancement

EXPERIMENTS

Distribution Perception and Generation

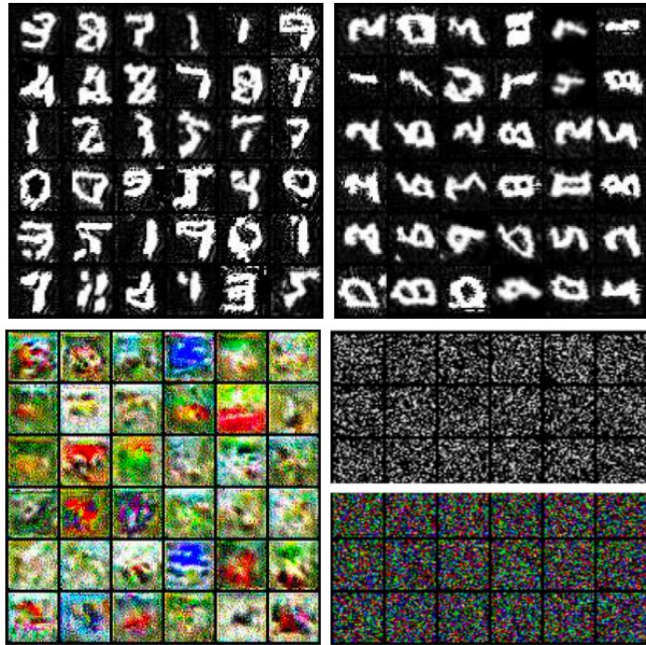


Figure 4. Test distribution perception visualization for identical training and testing distributions on MNIST and CIFAR-10.

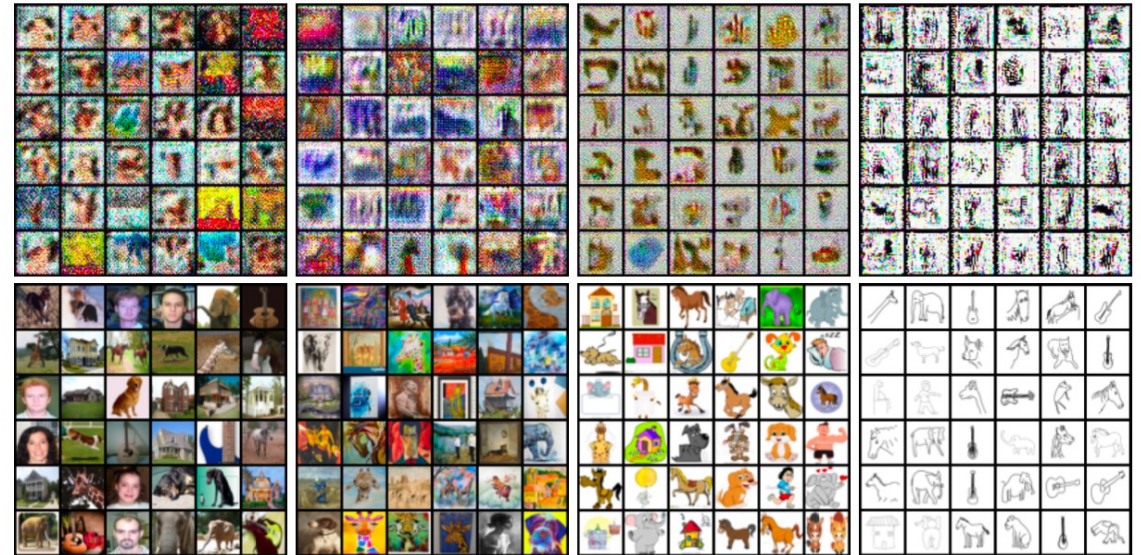


Figure 5. Test distribution perception visualization (**upper**) and real samples (**lower**) on shifted distribution: A model trained on PACS-A dataset then individually tested with TEA adaptation across PACS-P, PACS-A, PACS-C, PACS-S datasets.

Figure: TEA's Distribution Perception and Generation

EXPERIMENTS

Distribution Perception and Generation

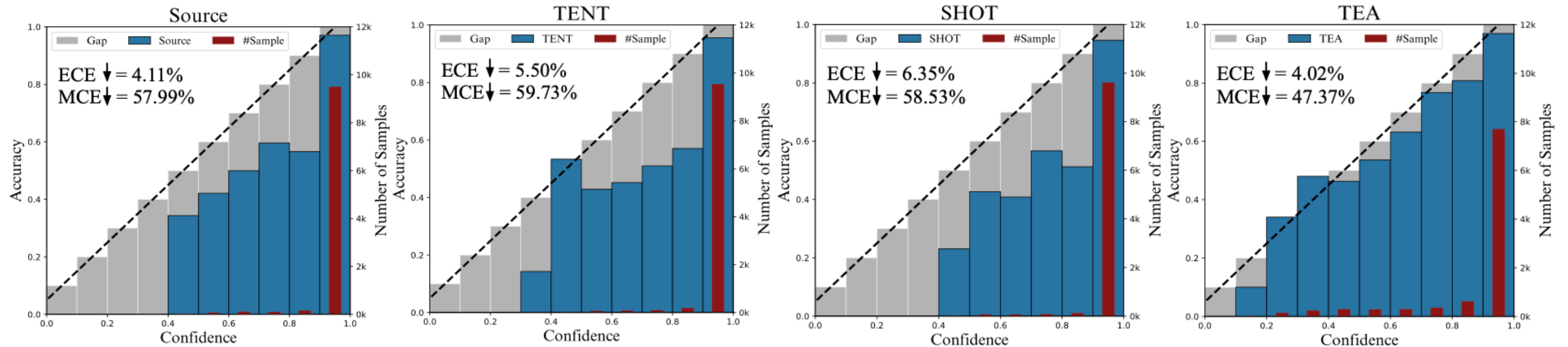


Figure 6. Calibration comparison between TEA and baselines on CIFAR-10 dataset. In an ideal scenario for optimal calibration, blue bars should align with the diagonal line, and a smaller grey gap area is preferred. Quantitative measures are provided via ECE and MCE metrics, where lower values indicate better calibration.

Figure: TEA's Improvements in Confidence Calibration



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- Trustworthy AI



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- Graph Neural Networks
- Network Embedding



Liang Hou

- Generative Adversarial Nets
- Generative Models



Fei Sun

- Recommender Systems
- Natural Language Processing



Huawei Shen

- Network Data Mining
- Social Network Analysis
- Graph Neural Networks



Xueqi Cheng

- Network Data Science
- Social Computing
- Information Retrieval



Thank you for your attention!

Paper



Code



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